

CLASS:XII	INDIAN SCHOOL MUSCAT SECOND PERIODIC ASSESSMENT Marking Scheme	SUBJECT: MATHEMATICS
Q. NO.	SET - C VALUE POINTS	SPLIT UP OF MARKS
1	$y = \tan^{-1} \frac{\sqrt{1+x^2} - 1}{x}$, put $x = \tan \theta$ $y = \tan^{-1} (\tan \frac{\theta}{2})$ $= \frac{1}{2} \tan^{-1} x$ $\therefore \frac{dy}{dx} = \frac{1}{2(1+x^2)}$	Each step carries $\frac{1}{2}$ mark
2.	$x = a(\theta + \sin \theta)$; $y = a(1 - \cos \theta)$ $\frac{dx}{d\theta} = a(1 + \cos \theta)$; $\frac{dy}{d\theta} = a \sin \theta$ $\frac{dy}{dx} = \tan \frac{\theta}{2}$ $\therefore \left(\frac{dy}{dx} \right)_{x=\frac{\pi}{3}} = \frac{1}{\sqrt{3}}$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
3.	Let $g(x) = \cos x$ and $h(x) = x^2$ $f = g \circ h$ g and h are continuous function conclusion	Each step carries $\frac{1}{2}$ mark
4.	Finding LHL and RHL Conclusion	$1\frac{1}{2}$ $\frac{1}{2}$
5.	$y = (\sin^{-1} x)^2$ Differentiating both sides w.r.t.x, $\Rightarrow \frac{dy}{dx} = \frac{2 \sin^{-1} x}{\sqrt{1-x^2}}$ $\Rightarrow \sqrt{1-x^2} \frac{dy}{dx} = 2 \sin^{-1} x$ Squaring & differentiating both sides w.r.t.x and proving	$1\frac{1}{2}$ $2\frac{1}{2}$

<p>6.</p> <p>f is continuous at $x = 2$ and $x = 10$</p> <p>Continuity at $x = 2$</p> <p>$\Rightarrow 2a + b = 5$----- (i)</p> <p>Continuity at $x = 10$</p> <p>$\Rightarrow 10a + b = 21$----- (ii)</p> <p>Solving (i) & (ii)</p> <p>Final answer : $a = 2$ & $b = 1$</p>	<p>Each step carries 1 mark</p>
<p>7.</p> <p>Let $u = x^{\sin x}$ and $v = (\sin x)^{\cos x}$</p> <p>$\Rightarrow y = u + v \Rightarrow \frac{dy}{dx} = \frac{du}{dx} + \frac{dv}{dx}$</p> <p>$\frac{du}{dx} = x^{\sin x} \left[\cos x \log x + \frac{\sin x}{x} \right]$----- (i)</p> <p>$\frac{dv}{dx} = (\sin x)^{\cos x} \left[-\sin x \log \sin x + \cos x \cot x \right]$----- (ii)</p> <p>$\therefore \frac{dy}{dx} = x^{\sin x} \left[\cos x \log x + \frac{\sin x}{x} \right] + (\sin x)^{\cos x} \left[-\sin x \log \sin x + \cos x \cot x \right]$</p>	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>